

**MATH 527: GEOMETRY/TOPOLOGY I**

FALL 2006

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HOMEWORK # 9; November 20, 2006

Complex manifolds, Lie groups

Due on Monday November 27

42. Give a detailed proof that any complex manifold is orientable.
43. Find a polynomial in two complex variables whose zero set is a complex curve homeomorphic to the sphere with two handles.
44. Let  $M$  is a complex manifold and suppose  $X$  is a nonvanishing vector field on  $M$ . Prove that there exists another nonvanishing vector field  $Y$  linearly independent of  $X$ .
45. Represent the torus  $\mathbb{T}^n$  as a linear group.
46. Prove that the group of affine transformations of  $\mathbb{R}^n$  is isomorphic to a Lie subgroup of  $GL(n+1, \mathbb{R})$ . Calculate its dimension.